as well as Ru at both positions can be understood, since the ions have almost the same radii, 0.605 and 0.620 Å respectively (Shannon, 1976), and both $BaTiO₃$ and $BaRuO₃$ occur with the 6L structure.

The distance between the metal atoms in the $[Ru(1), Ti(2)]$, O_0 group is too short to form regular face-shared octahedra. Because of the repulsion between the metal atoms, they are not exactly at the centers of the face-sharing octahedra. This results in a shorter $O(1)$ - $O(1)$ distance in the common face and in the angle $O(1)$ -metal- $O(2)$ being larger than 90°.

The metal-metal distance is very short (2.515 Å) , suggesting intermetallic bonding. This intermetallic bond is also reported in the $9L$ -BaRuO, structure, in which the Ru--Ru distance is 2.55 Å (Donohue, Katz & Ward, 1965).

In $Ba_3SrNb_2O_9$ (Zandbergen & IJdo, 1983) the Nb-Nb distance is 2.97 Å, while in $Ba_3SrRu_2O_9$ (Zandbergen & IJdo, 1984) the Ru-Ru distance is 2.67 A. This difference is due to the atomic radius of $Nb⁵⁺$, which is larger than that of $Ru⁵⁺$, 0.64 Å and $0.565~\text{\AA}$ respectively (Shannon, 1976). The difference in Ru-Ru distance in $Ba_3TiRu_2O_9$ and $Ba_3SrRu_2O_9$ is probably the result of the difference in valence of the Ru atoms, which is respectively $4+$ and $5+.$

In an undeformed packing with ideal octahedra the axial ratio $c/a = \sqrt{6} = 2.449$ (Zandbergen & IJdo, 1983). For $Ba_3TiRu_2O_9$ the axial ratios are 2.455 at 300 K and 2.456 at 1.2 K. A tilt around the threefold

axes decreases the lattice parameter a and thus increases *c/a.* Because the *c/a* values are close to the expected value, we expect that the tilt is zero.

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Structure of the Intermediate Phase, $\text{Li}_{2.09}\text{W}_{0.91}\text{Nb}_{0.09}\text{O}_4$ **, in the** $\text{Li}_2\text{WO}_4-\text{Li}_3\text{NbO}_4$ **System**

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Abstract. $M_r = 254.2$, triclinic, $P\bar{1}$, $a = 7.967$ (2), $b=7.774$ (1), $c=5.271$ (1) Å, $\alpha=90.61$ (2), $\beta=$ 103.41 (2), $\gamma = 105.81$ (2)^o, $V = 304.6$ (1) Å³, $Z = 4$, $D_m = 5.518$, $D_x = 5.543$ (2) g cm⁻³, λ (Mo $K\alpha$) = 0.71069 A, $\mu = 367$ cm⁻¹, $F(000) = 437$, $T = 293$ K, final $R = 0.047$ for 2125 observed reflections. The O atoms are in approximate cubic close-packing with (W,Nb) atoms in octahedral interstices, arranged so that $(W, Nb)₄O₁₆$ groups are created. These groups are connected through a three-dimensional framework of edge-sharing LiO_6 octahedra and Li_4O_{10} groups of edge-sharing LiO₄ tetrahedra.

Introduction. The niobium-tungsten oxides containing alkali metals are of considerable interest as solid-state ionic conductors. $Li⁺$ ions especially have been shown to be mobile in a voltage gradient, and therefore the Li-W-Nb-O system has been investigated at this laboratory (Hörlin, Marinder & Nygren, 1982).

The subsystem $Li_2WO_4 - Li_3NbO_4$ was searched for non-stoichiometric compounds with partially occupied lithium sites. The phase analysis revealed one intermediate compound, which could be prepared as a single phase, with the composition $Li_{2,09}W_{0.91}Nb_{0.09}O_4$. This article will describe the results of the single-crystal

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X-ray structure determination. The conductivity measurements will be published elsewhere.

Experimental. Starting materials: $Li,WO₄$ and $Li₃NbO₄$, prepared by heating appropriate amounts of $Li₂CO₃$ (Mallinckrodt, analytical reagent), WO₃ (99.9% pure, Koch-Light Lab.) and $Nb₂O₅$ (Merck, optipure, purified of oxide fluorides at 1275 K in air) in Pt crucibles at 875 K, one week. Purity checked by analysis of X-ray powder patterns. Single-phase sample, composition $Li_{2.09}W_{0.91}Nb_{0.09}O_4$, confirmed by density measurements, obtained by mixing $Li₂WO₄$ and $Li₃NbO₄$ in the mole-ratio 10:1 and kept in sealed Pt ampoules at 1175 K, two days. Unit-cell dimensions from Guinier X-ray powder pattern,* refined with program *PIRUM* (Werner, 1969), internal standard KCI ($a = 6.2930$ Å at 298 K, Hambling, 1953). Density determined from apparent loss of weight in n-hexane, density of the liquid calibrated with Ge crystal $(D = 5.326 \text{ g cm}^{-3})$ at 298 K (Straumanis & Aka, 1952).

Diffraction data from a small, irregular, colourless single crystal mounted on a Philips PW 1100 computercontrolled automatic four-circle diffractometer with a graphite monochromator. Data corrected for Lorentz and polarization as well as absorption effects; anomalous-scattering-factor values for uncharged atoms from *International Tables for X-ray Crystallography* (1974); calculations performed with *SHELX76* (Sheldrick, 1976) on the Amdahl 470/7A and VAX computing systems. Details of data collection and refinement are given in Table I.

Solution of structure with Patterson and difference Fourier methods, refinement by full-matrix leastsquares techniques (based on F) in space group \overline{PI} . Heavy metals treated as W. Occupational parameters determined for W and Li by alternate refinements of isotropic thermal parameters and occupancy factors. 0.95 (1) for W agreed well with the 0.96 derived from density measurements. 7.1 out of 8.36 Li atoms found, the rest is probably randomly distributed over some of the available octahedral and tetrahedral interstices. $(d/\sigma)_{\text{max}} = 0.005$, $(d\rho)_{\text{max}} = 4.6$ e A⁻³ (in the vicinity of W) and $(\Delta \rho)_{\min} = -4.9 \text{ e A}^{-3}$ in final difference Fourier map. E statistics as a function of sin θ/λ gave the value 0.82, intermediate between the theoretical values 0-97 for centrosymmetry and 0.74 for noncentrosymmetry (Karle, Dragonette & Brenner, 1965). Attempts to refine the structure in the noncentrosymmetric space group (P1) resulted in an increase in e.s.d.'s by 50% and a decrease of the R value from 0.047 to 0.044. The structure is thus probably best described in \overline{PI} .

Table 1. *Details of the data collection and refinement*

Discussion. The final positional, thermal and occupancy parameters are given in Table 2. Relevant interatomic distances are presented in Table 3.*

The structure of $Li_{2.09}W_{0.91}Nb_{0.09}O_4$, thus derived, can be described as a distorted cubic close-packed arrangement of O atoms. The (W,Nb) atoms occupy $\frac{1}{4}$ of the octahedral interstices, and the Li atoms are distributed over $\frac{1}{4}$ of the octahedrally and $\frac{1}{8}$ of the tetrahedrally coordinated sites. The structure is composed of identical sheets of metal-oxygen polyhedra, as is shown in Fig. 1. The sheets are stacked on top of each other and shifted so that identically numbered O atoms coincide. The (W,Nb) atoms are arranged in $(W, Nb)₄O₁₆$ tetramers of edge-sharing $(W, Nb)O₆$ octahedra, connected through Li_4O_{10} tetramers of edgesharing $LiO₄$ tetrahedra and rows of four edge-sharing $LiO₆$ octahedra. The lithium--oxygen polyhedra form a three-dimensional framework, since the $LiO₆$ octahedra rows are also joined to each other by edge-sharing in a staircase-like way perpendicular to the projection plane of the structure *(cf* Fig. 2a).

The metal-metal repulsion within the $(W, Nb)₄O₁₆$ group is obvious (Fig. 2b). The metal atoms are shifted from the centres of the octahedra so that shorter bonds $(1.78-1.80 \text{ Å})$ are formed to the O atoms not shared with other $(W, Nb)O₆$ octahedra. The two- and threecoordinated O atoms are bonded to the (W,Nb) atoms with distances ranging from 1.89 to 2.24 Å. The same distribution of bond distances has been found in the compounds $Li_2WO_4(III)$ (Wilhelmi, Waltersson & Löfgren, 1977) and Ag_2WO_4 (Skarstad & Geller, 1975), both having structures containing this kind of M_4O_{16} tetramer. The short O-O distances (2.51- 2.64 Å) appear as shared edges, which is normal with most transition-metal-anion polyhedra involved in such types of linking in accordance with one of Pauling's

^{*}JCPDS Diffraction File No. 35-1498. See also deposition footnote.

^{*} Lists of structure factors and the indexed powder pattern have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 39781 (31 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

Table 2. *Positional and thermal parameters*

Standard deviations are given within parentheses.

Anisotropic thermal parameters are given in the form: $exp{-2\pi^2(h^2a^*U_{11} + k^2b^*U_{22} + Pc^*U_{33} + 2hka^*b^*U_{12} + 2hla^*c^*U_{13} + 2hab^*D^*U_{14} + 2hab^*D^*U_{15} + 2hab^*D^*U_{16}}$ $2klb^*c^*U_{23}$.

Table 3. *Relevant interatomic distances in A*

Standard deviations are given within parentheses.

rules (Pauling, 1960). The distortion of the oxygen lattice gives rise to elongated octahedral interstices containing two crystallographically independent Li atoms $[Li(1)$ and $Li(2)$.

The $Li(2)O₆$ octahedron shows a relatively small scatter in Li(2)-O bond lengths $(2.06-2.21 \text{ Å})$, although the O-O distances vary from 2.64 to 3.44 A. In the Li(1) O_6 octahedron the Li atom is displaced from the centre so that four short $(2.00-2.13 \text{ Å})$ and two long bonds $(2.30 \text{ and } 2.52 \text{ Å})$ arise. The coordination polyhedron may thus also be described as a very distorted tetrahedron. The O-O distances within this octahedron range from 2.70 to 3.39 A.

The $Li(3)$ and $Li(4)$ atoms occupy tetrahedrally coordinated sites, and two of each kind form an $Li₄O₁₀$

Fig. 1. Two consecutive layers of the idealized cubic close-packed structure of $Li_{2.09}W_{0.91}Nb_{0.09}O_4$. (I is the lower layer and II is the upper layer.) Filled circles represent (W,Nb). Empty octahedra and tetrahedra correspond to $LiO₆$ and $LiO₄$ polyhedra respectively. The Li atoms have been excluded for clarity. The numbers refer to some of the O atoms connecting the two layers shown.

tetramer of edge-sharing tetrahedra. The $Li-O$ distance-ranges within the tetrahedra are $1.91-1.99 \text{ Å}$ and $1.94-2.20$ Å, respectively. The O-O distances vary from 2.93 to 3.45 Å in the $Li(3)O₄$ and from 2.93 to 3.58 Å in the $Li(4)O₄$ tetrahedron. The longest distance corresponds to the outer edge of the tetramer, and the shorter distances are found between O atoms involved in edge-sharing.

Analogous kinds of elongated $LiO₆$ octahedra, with two long Li-O distances $(2.30-2.58 \text{ Å})$, have been observed in several compounds with close-packed anion lattices, such as $Li₂WO₄(II)$ (Waltersson, Werner &

Wilhelmi, 1977; Horiuchi, Morimoto & Yamaoka, 1979), Li₂WO₄(IV) (Horiuchi, Morimoto & Yamaoka, 1980) and L -Li₂Mo₄O₁₃ (Gatehouse & Miskin, 1974). A somewhat more regular $LiO₆$ octahedron appears in the hexagonally close-packed structure of $LiNb₃O₈$ (Lundberg, 1971), with Li-O distances between 2.08 and $2.34 \text{ Å}.$

The atomic distances within the $LiO₄$ tetrahedra are similar to those found in the structures of $Li₂WO₄(II)$ and Li_yW₂O₇ (Okada, Morikawa, Marumo & Iwai, 1975), although the longest $O-O$ distance, 3.58 Å, is rather long.

The metal-to-oxygen ratio of $Li_{2.09}W_{0.91}Nb_{0.09}O_4$ is very close to that of $Li₂WO₄$. At room temperature and atmospheric pressure the latter compound, called $Li₂WO₄(I)$ (Zachariasen & Plettinger, 1961), adopts the phenacite structure type $(Be, SiO₄)$. The O atoms are spaciously arranged, and both Li and W are tetrahedrally coordinated.

Through exchange of small amounts of tungsten for niobium, as is the case in the present compound, a distorted close-packed array of O atoms is obtained. Close-packing of O atoms in $Li₂WO₄$ can also be achieved by increasing the pressure and temperature.

Three high-pressure phases have been found, of which $Li₂WO₄(II)$ has a structure built up of cubic close-packed O atoms with the Li atoms octahedrally and tetrahedrally coordinated. $Li₄O₁₂$ rings of cornersharing $LiO₄$ tetrahedra and $LiO₆$ octahedra connect the W_4O_{16} groups of edge-sharing WO_6 octahedra into a three-dimensional framework.

The structures of Li₂WO₄(III) (Wilhelmi *et al.,* 1977) and Li₂WO₄(IV) (Horiuchi *et al.*, 1980) are both based on a hexagonally close-packed oxygen network, but the metal atoms are distributed in different manners. A complete structure determination of $Li,WO₄(III)$ has not been reported, although Wilhelmi *et al.* determined the tungsten-oxygen arrangement. The W atoms are

Table 4. *Experimental conditions and oxygen packing in the Li*₂WO₄ *polymorphs and Li*_{2.09}W_{0.91}Nb_{0.09}O₄

Compound	P(GPa)	T(K)	Oxygen arrangement $V(\dot{A}^3)/O$	
Li,WO, (I)	$\sim 10^{-4}$	775	Phenacite-	23.8
(Zachariasen & Plettinger,			type	
1961)				
Li , WO , (II)	0.3	900	c.c.p.	18-8
(Horiuchi et al., 1979)				
Li,WO, (III)	2	$1375 \rightarrow 920$	h.c.p.	18-6
(Wilhelmi et al., 1977)				
Li,WO, (IV)	4	1125	h.c.p.	18-1
(Horiuchi et al., 1980)				
$Li_{2.09}(W, Nb)O_4$	$~10^{-4}$	1175	c.c.p.	$19-0$
(present work)				

located in octahedral interstices ordered in such a way that four $WO₆$ octahedra share edges and form $W₄O₁₆$ groups, of a type different from those in $Li_3WO_4(II)$, however.

In the structure of $Li₂WO₄(IV)$ the WO₆ octahedra are joined by edge-sharing to form infinite zigzag strings as in the orthorhombic form of $PbO₂$. The Li atoms exclusively occupy octahedral sites so that two-dimensionally infinite sheets of edge-sharing distorted $LiO₆$ octahedra are formed. The sheets are joined by the zigzag strings of $WO₆$ octahedra.

In spite of the similarities between $Li_{2.09}$ - $W_{0.91}Nb_{0.09}O_4$ and $Li_2WO_4(II)$ with respect to the c.c.p, oxygen network and the type of coordination polyhedra surrounding the metal atoms, the modes of coupling of the LiO₄ tetrahedra to Li₄O₁₀ and Li₄O₁₂ tetramers, respectively, are of different kinds. The W_4O_{16} tetramers are also different. However, the W_4O_{16} group in $Li_{2,09}W_{0.91}Nb_{0.09}O_4$ can be recognized in Li , $WO₄(III)$.

As can be seen in Table 4, the density of the oxygen packing is increased by applying high pressure on $Li₂WO₄(I)$ of phenacite structure type. It is interesting to note that a close-packed oxygen arrangement can also be obtained when a small amount of tungsten is replaced by the same amount of niobium.

Fig. 2. (a) The framework of Li-O polyhedra and (b) the $(W, Nb)₄O₁₆$ group viewed perpendicular to the close-packed oxygen layers.

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Structure of Metastable Lead Metavanadates: the Monoclinic PbV₂O₆(II) Modification

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Abstract. $M_r = 405.07$, monoclinic, $C2/m$, $a =$ 15.525 (2), $b = 3.6960$ (6), $c = 9.436$ (4) Å, $\beta =$ 110.44 (1)^o, $V = 507.3$ (2) \mathbf{A}^3 , $Z = 4$, $D_r =$ 5.30 Mg m⁻³, $\lambda(Mo K\alpha) = 0.71069 \text{ Å}, \qquad \mu =$ $36 \cdot 75$ mm⁻¹, $F(000) = 704$, $T = 293$ K; final $R =$ 0.046 for 313 observed reflections. All the atoms lie on mirror planes. The structure of $PbV₂O₆(II)$ differs from that of other MX_2O_6 systems and consists of columns of double chains of edge-sharing VO_5 square pyramids which extend infinitely along the b axis; Pb atoms are interspersed.

Introduction. Recent studies on the equimolar PbO.V₂O₅ system (Calestani, Montenero, Pigoli & Bettinelli, 1984) show the existence of two new lead metavanadate phases, which crystallize from the melt when the cooling rate is extremely high; they are imbedded in a vitreous matrix. These phases, indicated as $PbV_2O_6(II)$ and (III), are metastable at room temperature and present structures which differ from that of all other MX_2O_6 systems. Both transform on heating to the well known stable phase $PbV_2O_6(I)$ (Jordan & Calvo, 1974) and must be considered as an intermediate lattice arrangement between the stable form and the glass.

The crystal-structure analysis of these compounds is therefore quite interesting for the comprehension of the structural evolution leading to the vitreous state. We present here the structural study of $PbV_2O_6(II)$, *i.e.* of the first step of this transition between the ordered and disordered state.

Experimental. PbV₂ $O_6(II)$ can be obtained imbedded in a vitreous matrix by quenching near equimolar

PbO.V₂O₅ melts on a steel vessel. Because of the tendency of the glass, at this cooling rate, to enrich itself in V_2O_5 , the separation of crystalline PbV₂O₆(II) from the glass is followed by the formation of PbV_2O_7 (chervetite) for a V_2O_5/PbO molar ratio less than 1.2.

The separation of $PbV₂O₆(II)$ single crystals from the quenched mass was quite difficult, since polycrystalline agglomerates appear, because of the high growth rate, as a compact mass in which the single components are practically indistinguishable. In spite of this, some small dark-brown crystals could be isolated by repeatedly breaking the samples.

Intensity data collected from a twin member of a small needle crystal $(0.03 \times 0.03 \times 0.2 \text{ mm})$, automated Philips PW 1100 four-circle diffractometer, graphite-monochromated Mo K α radiation, 2-30° θ range, max. range h, k, l : 20,5,12, θ -2 θ scan, 1.4° scan width, 0.1° s⁻¹ scan rate; backgrounds estimated from 5 s counts at each end of scan. Lattice parameters determined by least-squares refinement of setting angles of 16 reflections in range $9 < \theta < 18^{\circ}$. One standard reflection (020), max. intensity variation 2.2%. 882 reflections measured of which 353 with $I > 3\sigma(I)$ considered observed and after correction for Lorentz and polarization effects resulted in 313 unique reflections, $R_{\text{int}} = 0.042$. The strong high- χ (~90°) 002 and 004 reflections were not included in the list because of overlap with reflections from other twins. The absorption correction performed by the ψ -scan method (North, Phillips & Mathews, 1968) was affected by the same phenomenon and therefore was not utilized in the structure analysis. All calculations performed on a Gould SEL 32/77 computer using a local version of *SHELX76* (Sheldrick, 1976). Structure solved by

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